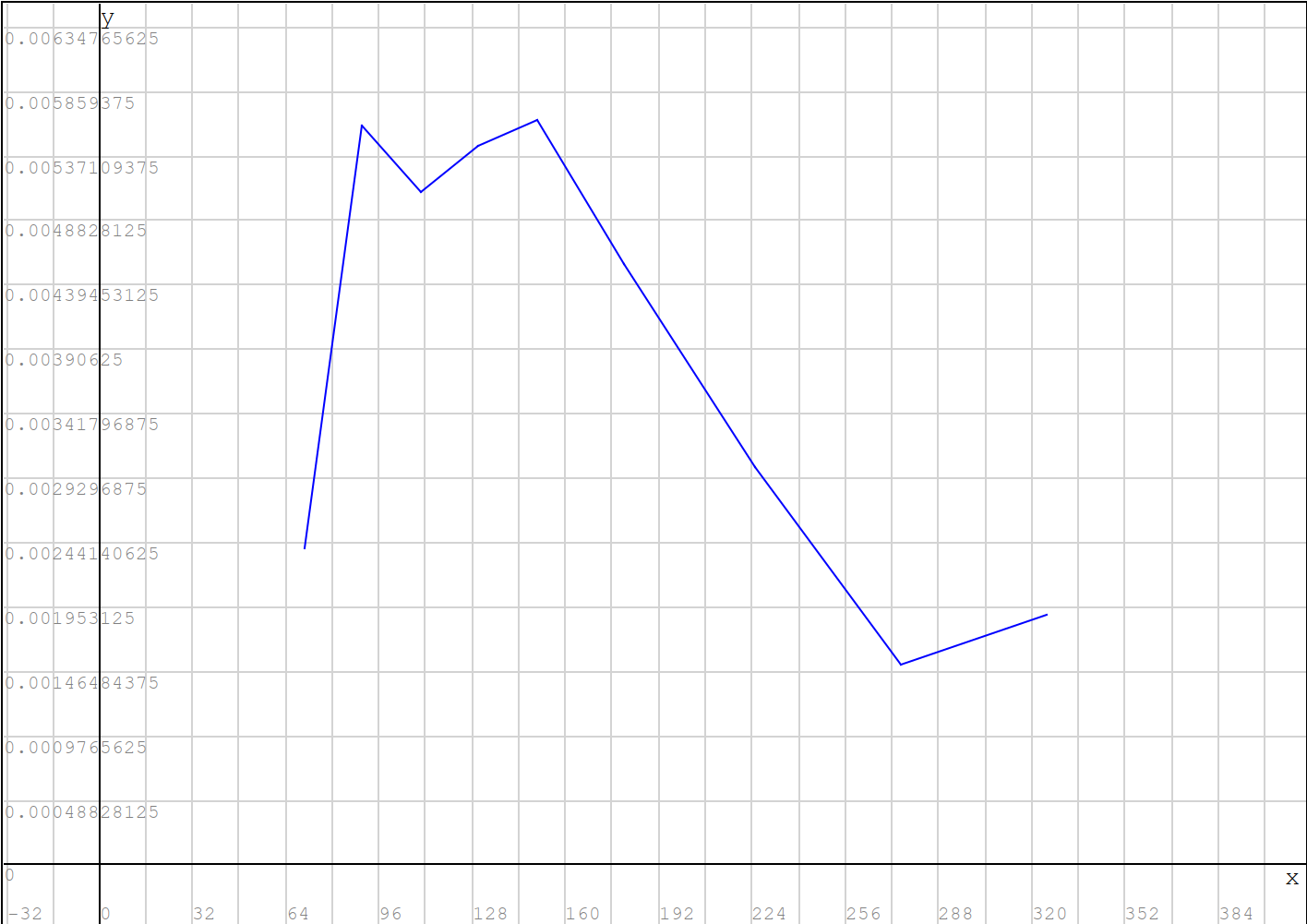


underlying data

$$x := \begin{bmatrix} 70 \\ 90 \\ 110 \\ 130 \\ 150 \\ 180 \\ 225 \\ 275 \\ 325 \end{bmatrix}$$

$$y := \begin{bmatrix} 0.0024 \\ 0.0056 \\ 0.0051 \\ 0.00545 \\ 0.00565 \\ 0.00455 \\ 0.00302 \\ 0.00152 \\ 0.0019 \end{bmatrix}$$

$$g1(x) := \begin{bmatrix} 70 & 0.0024 \\ 90 & 0.0056 \\ 110 & 0.0051 \\ 130 & 0.00545 \\ 150 & 0.00565 \\ 180 & 0.00455 \\ 225 & 0.00302 \\ 275 & 0.00152 \\ 325 & 0.0019 \end{bmatrix}$$



$g1(x)$

we introduce a formula for the approximation $a1 := \text{eval}(100 \cdot \sqrt{2 \cdot \pi})$

$$wb := \left(\frac{h1}{\sigma1 \cdot a1} \right) \cdot \exp \left(- \frac{(x - \mu1)^2}{2 \cdot \sigma1^2} \right) + \left(\frac{h2}{\sigma2 \cdot a1} \right) \cdot \exp \left(- \frac{(x - \mu2)^2}{2 \cdot \sigma2^2} \right) + \left(\frac{h3}{\sigma3 \cdot a1} \right) \cdot \exp \left(- \frac{(x - \mu3)^2}{2 \cdot \sigma3^2} \right)$$

initial values of 9 parameters

$$h1 := 0$$

$$h2 := 0$$

$$h3 := 0$$

$$\mu1 := 50$$

$$\mu2 := 100$$

$$\mu3 := 200$$

$$\sigma1 := 1$$

$$\sigma2 := 1$$

$$\sigma3 := 1$$

10 parameters that need to be calculated, we set arbitrary values for now

$$Sqmin := 1$$

$$hh1 := 0.15$$

$$hh2 := 0.7$$

$$hh3 := 0.40$$

$$\mu\mu1 := 90$$

$$\mu\mu2 := 160$$

$$\mu\mu3 := 350$$

$$\sigma\sigma1 := 19$$

$$\sigma\sigma2 := 50$$

$$\sigma\sigma3 := 80$$

The difference between the original data and those calculated by the formula

$$Raz(h1 ; h2 ; h3 ; \mu1 ; \mu2 ; \mu3 ; \sigma1 ; \sigma2 ; \sigma3) := \text{eval}(y - wb)$$

the sum of the squares of the deviations of the initial data from the desired function

$$Sq(h1 ; h2 ; h3 ; \mu1 ; \mu2 ; \mu3 ; \sigma1 ; \sigma2 ; \sigma3) := \sum \left(\overrightarrow{Raz(h1 ; h2 ; h3 ; \mu1 ; \mu2 ; \mu3 ; \sigma1 ; \sigma2 ; \sigma3)}^2 \right)$$

we iterate through the parameters to minimize the sum of the squared deviations

$t0 := \text{time}(0)$

```

loop := [
  "h1" 1 100
  "h2" 1 100
  "h3" 1 100
  "μ1" 51 200
  "μ2" 101 350
  "μ3" 201 500
  "σ1" 1 80
  "σ2" 1 100
  "σ3" 1 150
]

loop := augment(loop [1..9][1..3] ; col(loop ; 2))

```

Here in the loop, Sq should be calculated and compared with Sqmin. The parameters under which the condition is met are saved

```

for t ∈ [1..10]
  if secondary = 1 if t > 1
    loop := augment(loop [1..9] 1 ; col(loop ; 4) ; col(loop ; 3) ; col(loop ; 4))
  else
    loop := augment(loop [1..9][1..2] ; col(loop ; 4) ; col(loop ; 4))
  Sqmin := 1 otherwise
  for i# ∈ [9..1]

```

```

    ""
    for j# ∈ [(loop i# 2) .. (loop i# 3)]
      tmp# := col(loop ; 4)
      tmp# i# := j#
      [
        h1 := tmp# 1 h2 := tmp# 2 h3 := tmp# 3
        μ1 := tmp# 4 μ2 := tmp# 5 μ3 := tmp# 6
        σ1 := tmp# 7 σ2 := tmp# 8 σ3 := tmp# 9
      ]
      Sq := Sq(h1 ; h2 ; h3 ; μ1 ; μ2 ; μ3 ; σ1 ; σ2 ; σ3)
      {
        loop i# 4 := j# if Sq < Sqmin
        Sqmin := Sq
        secondary := 0
      }
      Sqmin := Sqmin otherwise

```

h1 := loop 1 4

for i# ∈ [1..9]

```

    for j# ∈ [(loop i# 4) .. (loop i# 3)]
      tmp# := col(loop ; 4)
      tmp# i# := j#
      [
        h1 := tmp# 1 h2 := tmp# 2 h3 := tmp# 3
        μ1 := tmp# 4 μ2 := tmp# 5 μ3 := tmp# 6
        σ1 := tmp# 7 σ2 := tmp# 8 σ3 := tmp# 9
      ]
      Sq := Sq(h1 ; h2 ; h3 ; μ1 ; μ2 ; μ3 ; σ1 ; σ2 ; σ3)
      {
        loop i# 4 := j# if Sq < Sqmin
        Sqmin := Sq
        secondary := 1
      }
      Sqmin := Sqmin otherwise

```

σ3 := loop 9 4

```

[
  hh1 := h1 · 0.01 hh2 := h2 · 0.01 hh3 := h3 · 0.01
  μμ1 := μ1 μμ2 := μ2 μμ3 := μ3
  σσ1 := σ1 σσ2 := σ2 σσ3 := σ3
]

```

Dear alles,
Thank you for correcting my mistake.
But the desired result still did not work.
There, for some reason, the search of options stopped at the value of hh1 = 0.01, respectively, and hh2 = 0.01, hh3 = 0.01. That is, h1, h2, and h3 were only checked when the value = 1.
Whereas I expected that the iteration of options should reach hh1 = hh2 = hh3 = 1, respectively h1 = h2 = h3 = 100.
For other parameters, it also seems that the search for options has not reached the end.
That is why the resulting graph shows a complete mismatch between the original data and the approximating formula.
I don't have an error in the If statement?
There I put continue in the else field.

loop =

```

[
  "h1" 44 48 48
  "h2" 8 8 8
  "h3" 100 100 100
  "μ1" 131 131 131
  "μ2" 350 350 350
  "μ3" 201 201 201
  "σ1" 67 67 67
  "σ2" 100 100 100
  "σ3" 150 150 150
]

```

$Sqmin := Sq(h1 ; h2 ; h3 ; \mu1 ; \mu2 ; \mu3 ; \sigma1 ; \sigma2 ; \sigma3)$

$Sqmin = 0.000006088469608$

Here the program should print the value of the smallest square of the deviation and the values of the 9 parameters at which this is achieved

$h1 = 48$	$h2 = 8$	$h3 = 100$	$hh1 = 0.48$	$hh2 = 0.08$	$hh3 = 1$
$\mu1 = 131$	$\mu2 = 350$	$\mu3 = 201$	$\mu\mu1 = 131$	$\mu\mu2 = 350$	$\mu\mu3 = 201$
$\sigma1 = 67$	$\sigma2 = 100$	$\sigma3 = 150$	$\sigma\sigma1 = 67$	$\sigma\sigma2 = 100$	$\sigma\sigma3 = 150$

$$wh1(x) := \frac{hh1}{\sigma\sigma1 \cdot \sqrt{2 \cdot \pi}} \cdot \exp\left(-\frac{(x - \mu\mu1)^2}{2 \cdot \sigma\sigma1^2}\right)$$

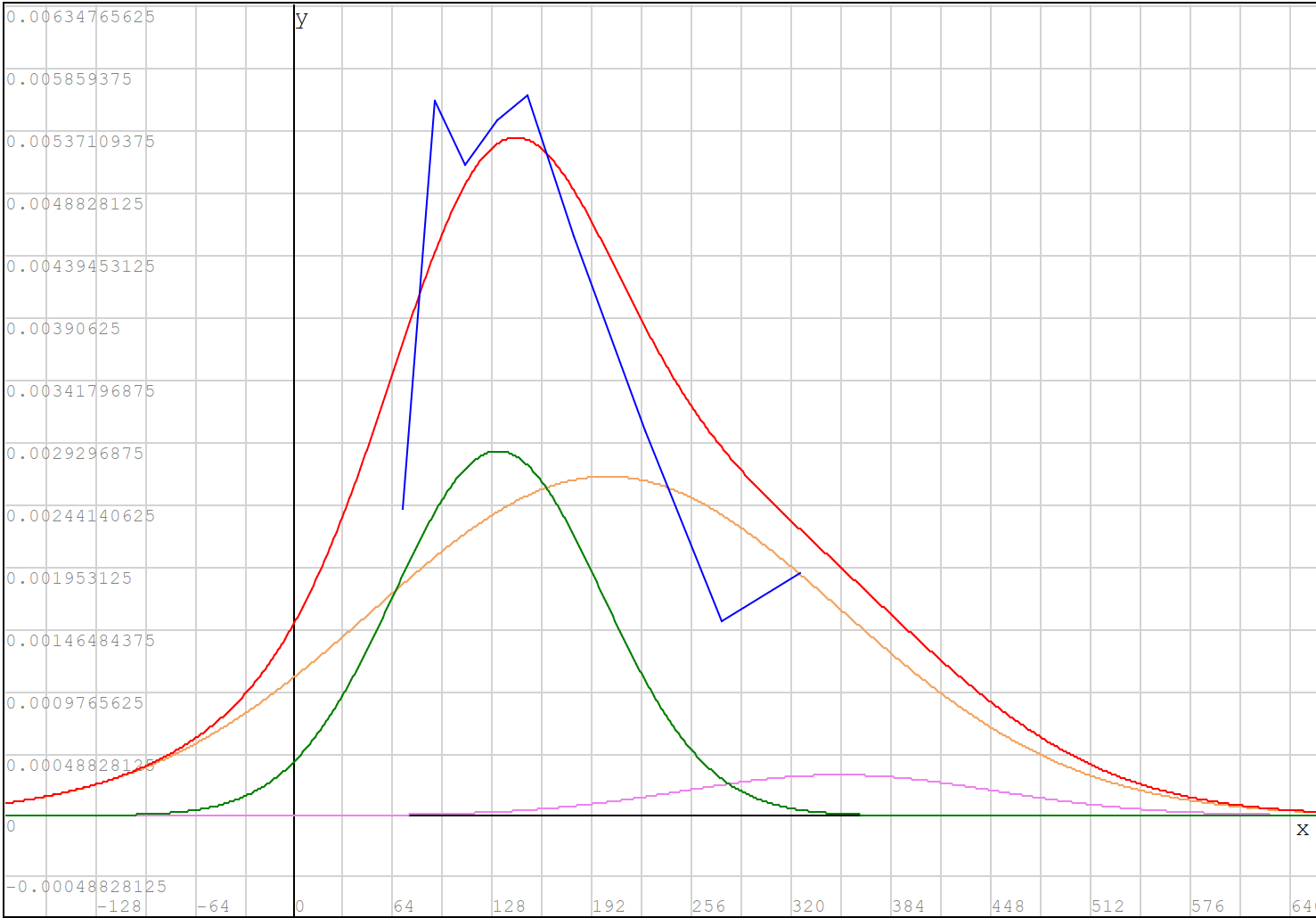
$$wh2(x) := \frac{hh2}{\sigma\sigma2 \cdot \sqrt{2 \cdot \pi}} \cdot \exp\left(-\frac{(x - \mu\mu2)^2}{2 \cdot \sigma\sigma2^2}\right)$$

$$wh3(x) := \frac{hh3}{\sigma\sigma3 \cdot \sqrt{2 \cdot \pi}} \cdot \exp\left(-\frac{(x - \mu\mu3)^2}{2 \cdot \sigma\sigma3^2}\right)$$

$$WW(x) := wh1(x) + wh2(x) + wh3(x)$$

Draw the resulting graphs.
Three normal distributions and their sum with different weights

$$time(1) - t0 = 468 \text{ s}$$



- $g1(x)$
- $WW(x)$
- $wh1(x)$
- $wh2(x)$
- $wh3(x)$